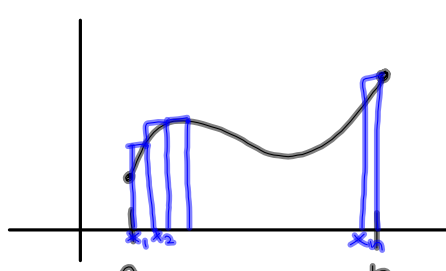


5.2



Area: base · height
 $\Delta x_n \cdot f(x_n)$

Sum: $\Delta x_1 \cdot f(x_1) + \Delta x_2 \cdot f(x_2) + \dots + \Delta x_n \cdot f(x_n)$

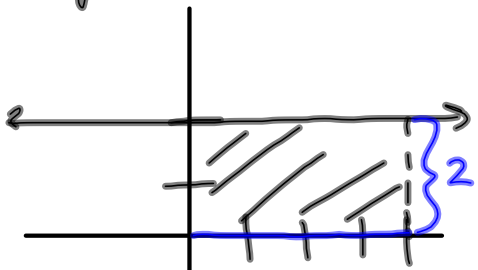
Exact: $\sum_{k=1}^n \Delta x_k \cdot f(x_k)$

$\lim_{n \rightarrow \infty} \sum_{k=1}^n \Delta x_k \cdot f(x_k)$ over $[a, b]$

$\int_a^b f(x) dx$

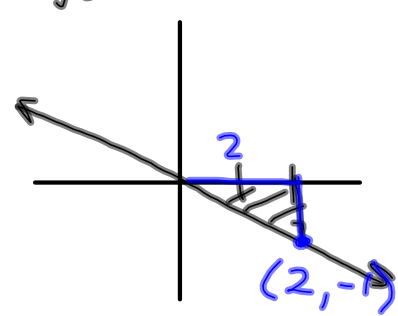
Jan 13-12:20 PM

1. $\int_0^4 2 dx = 8$



$A = bh = 4 \cdot 2 = 8$

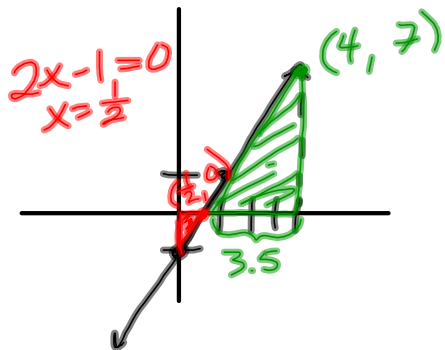
2. $\int_0^2 -\frac{1}{2}x dx$



$A = \frac{1}{2}(2)(-1) = -1$

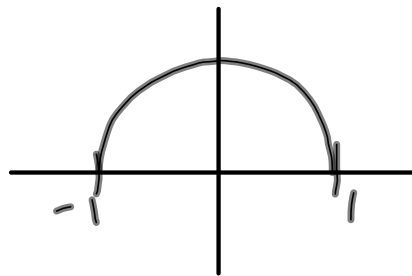
Jan 13-1:18 PM

3. $\int_0^4 (2x-1) dx$



$$A = \frac{1}{2}(\frac{1}{2})(-1) + \frac{1}{2}(3.5)(7) = 12$$

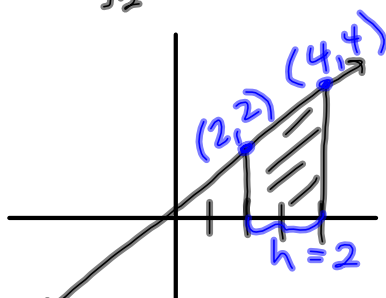
4. $\int_{-1}^1 \sqrt{1-x^2} dx$



$$A = \frac{1}{2}\pi r^2 = \frac{1}{2}\pi(1)^2 = \frac{\pi}{2}$$

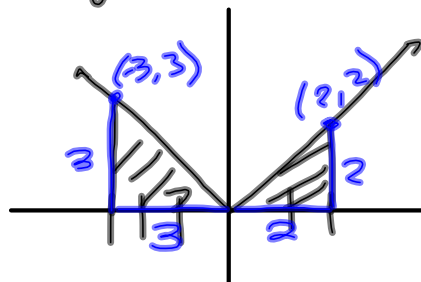
Jan 13-1:29 PM

5. $\int_2^4 x dx$



trapezoid
 $A = \frac{1}{2}(b_1 + b_2)h$
 $= \frac{1}{2}(2 + 4) \cdot 2$
 $= 6$

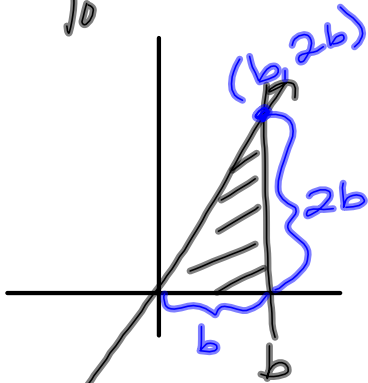
6. $\int_{-3}^2 |x| dx$



$$A = \frac{1}{2}(3)(3) + \frac{1}{2}(2)(2) = 6.5$$

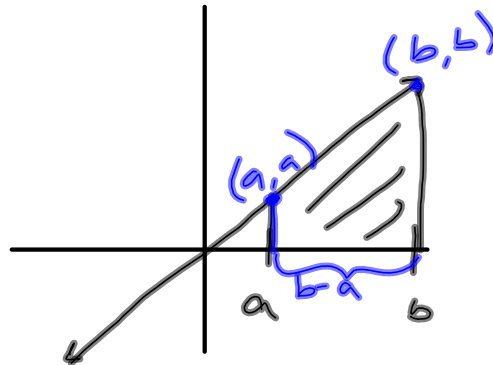
Jan 13-1:33 PM

$$7. \int_0^b 2x dx$$



$$A = \frac{1}{2}(b)(2b) \\ = b^2$$

$$8. \int_a^b x dx$$



$$A = \frac{1}{2}(a+b)(b-a) \\ = \frac{1}{2}(b^2 - a^2)$$

Jan 13-1:43 PM

$$9. \int_{-1}^3 x^2 dx = 9.333$$

Math \rightarrow fnInt \rightarrow enter

fnInt(x^2 , x , -1 , 3)
 fnc, variable, lower bound, upper bound

$$10. \int_0^\pi \sin x dx = 2$$

$$11. \int_{-3}^3 (9-x^2) dx = 36$$

Jan 13-1:47 PM