

$$29. \cot^2 x - \cos^2 x = \cos^2 x \cdot \cot^2 x$$

$$\text{LHS: } \frac{\cos^2 x}{\sin^2 x} - \frac{\cos^2 x}{1} \cdot \frac{\sin^2 x}{\sin^2 x}$$

$$\frac{\cos^2 x - \cos^2 x \sin^2 x}{\sin^2 x}$$

$$\frac{\cos^2 x \cdot (1 - \sin^2 x)}{\sin^2 x}$$

$$\cot^2 x \cos^2 x$$

Feb 1-2:16 PM

$$43. \cos^5 x = (1 - 2\sin^2 x + \sin^4 x)(\cos x)$$

$$\text{LHS: } \cos^5 x$$

$$\cos x (\cos^4 x)$$

$$\cos x (\cos^2 x)(\cos^2 x)$$

$$\cos x (1 - \sin^2 x)(1 - \sin^2 x)$$

$$\cos x (1 - 2\sin^2 x + \sin^4 x)$$

Feb 4-9:01 AM

$$27. \frac{\tan^2 x}{\sec x + 1} = \frac{1 - \cos x}{\cos x}$$

$$\text{LHS: } \frac{\sec^2 x - 1}{\sec x + 1}$$

$$\frac{(\sec x - 1)(\cancel{\sec x + 1})}{\cancel{\sec x + 1}}$$

$$\sec x - 1$$

$$\frac{1}{\cos x} - 1 \frac{\cos x}{\cos x}$$

$$\frac{1 - \cos x}{\cos x}$$

Feb 4-9:03 AM

5.3 Sum & Difference Identities

Obj: 1. Apply sum/difference identities to Sine, cosine, and tangent.

Sum / Difference

$$\sin(u \pm v) = \sin u \cos v \pm \cos u \sin v$$

$$\cos(u \pm v) = \cos u \cos v \mp \sin u \sin v$$

$$\tan(u \pm v) = \frac{\tan u \pm \tan v}{1 \mp \tan u \tan v}$$

Feb 4-9:09 AM

Find the exact value of $\cos 15^\circ$

$$\cos(45^\circ - 30^\circ)$$

$$= \cos 45^\circ \cos 30^\circ + \sin 45^\circ \sin 30^\circ$$

$$= \frac{\sqrt{2}}{2} \cdot \frac{\sqrt{3}}{2} + \frac{\sqrt{2}}{2} \cdot \frac{1}{2}$$

$$= \frac{\sqrt{6}}{4} + \frac{\sqrt{2}}{4} = \frac{\sqrt{6} + \sqrt{2}}{4}$$

Feb 4-9:36 AM

$$\sin 75^\circ$$

$$\sin(45^\circ + 30^\circ)$$

$$\sin 45^\circ \cos 30^\circ + \cos 45^\circ \sin 30^\circ$$

$$\frac{\sqrt{2}}{2} \cdot \frac{\sqrt{3}}{2} + \frac{\sqrt{2}}{2} \cdot \frac{1}{2}$$

$$\frac{\sqrt{6} + \sqrt{2}}{4}$$

Feb 4-9:40 AM

Prove: $\cos\left(\frac{\pi}{2} - x\right) = \sin x$

LHS:

$$\cos\frac{\pi}{2} \cos x + \sin\frac{\pi}{2} \sin x$$

$$0 \cdot \cos x + 1 \cdot \sin x$$

$$\sin x$$

Feb 4-9:43 AM

Write as a single expression of sine or cosine.

$$\sin 22^\circ \cos 13^\circ + \cos 22^\circ \sin 13^\circ$$

$$\sin(22^\circ + 13^\circ)$$

$$\sin(35^\circ)$$

Feb 4-9:45 AM